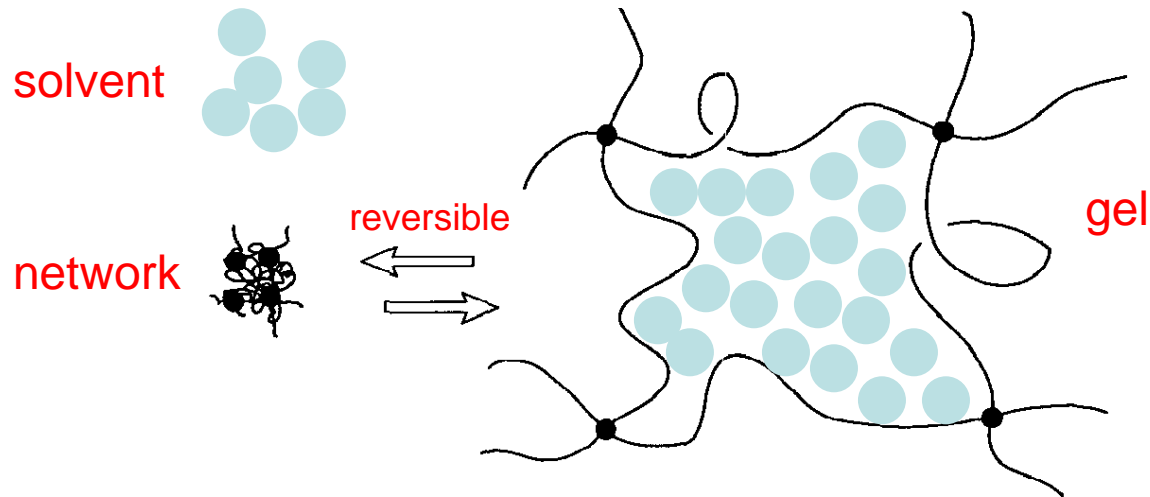


Soft Active Materials

dielectric elastomers
capable of
giant deformation of actuation

Zhigang Suo
Harvard University

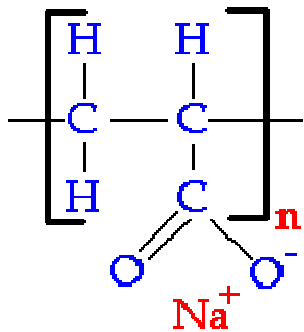
elastomer = network
gel = network + solvent



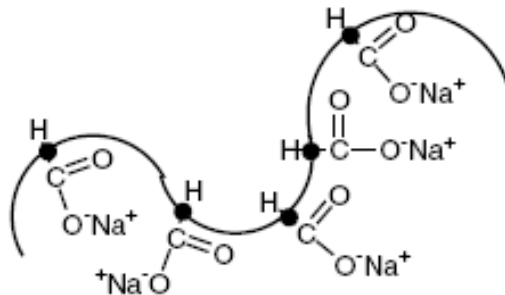
Super absorbent diaper



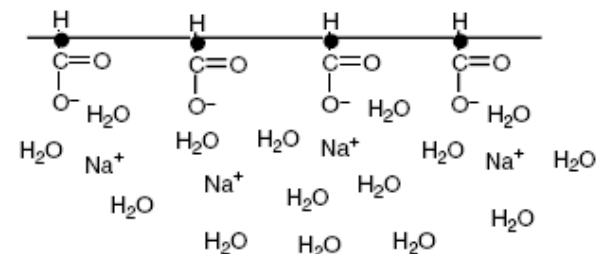
Sodium polyacrylate: **polyelectrolyte**



Dry



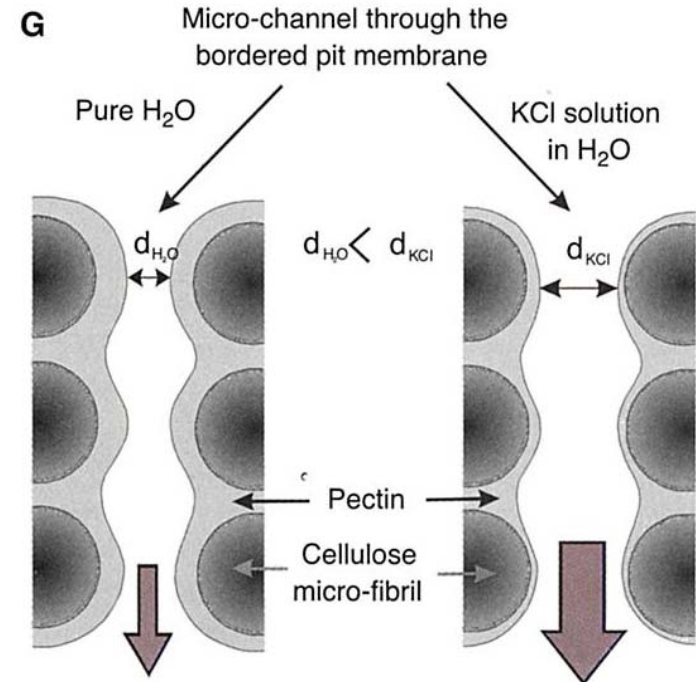
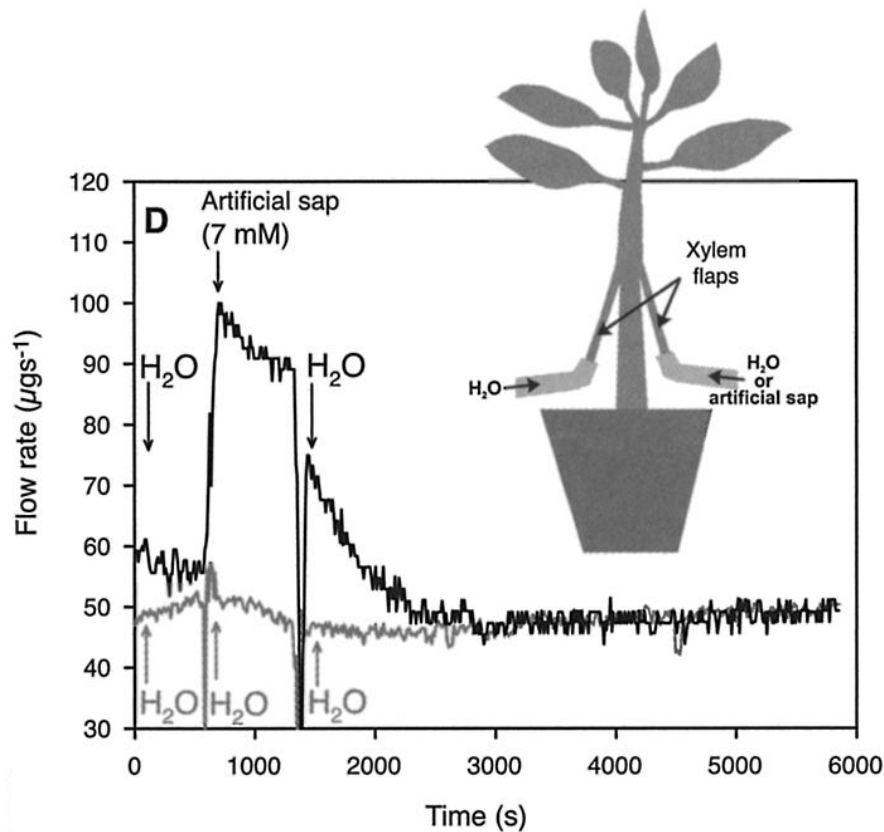
in Water



Gels regulate flow in plants



Missy Holbrook



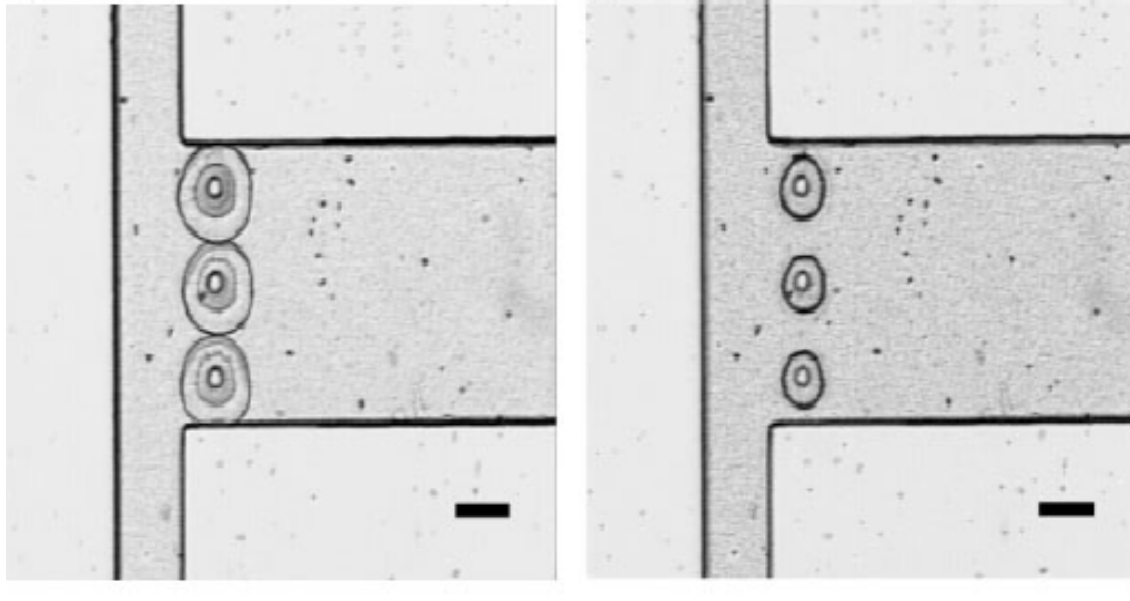
Zwieniecki, Melcher, Holbrook,
Hydrogel control of xylem hydraulic resistance in plants
Science 291, 1095 (2001)

Plants are masters of microfluidics

Self-regulating fluidics



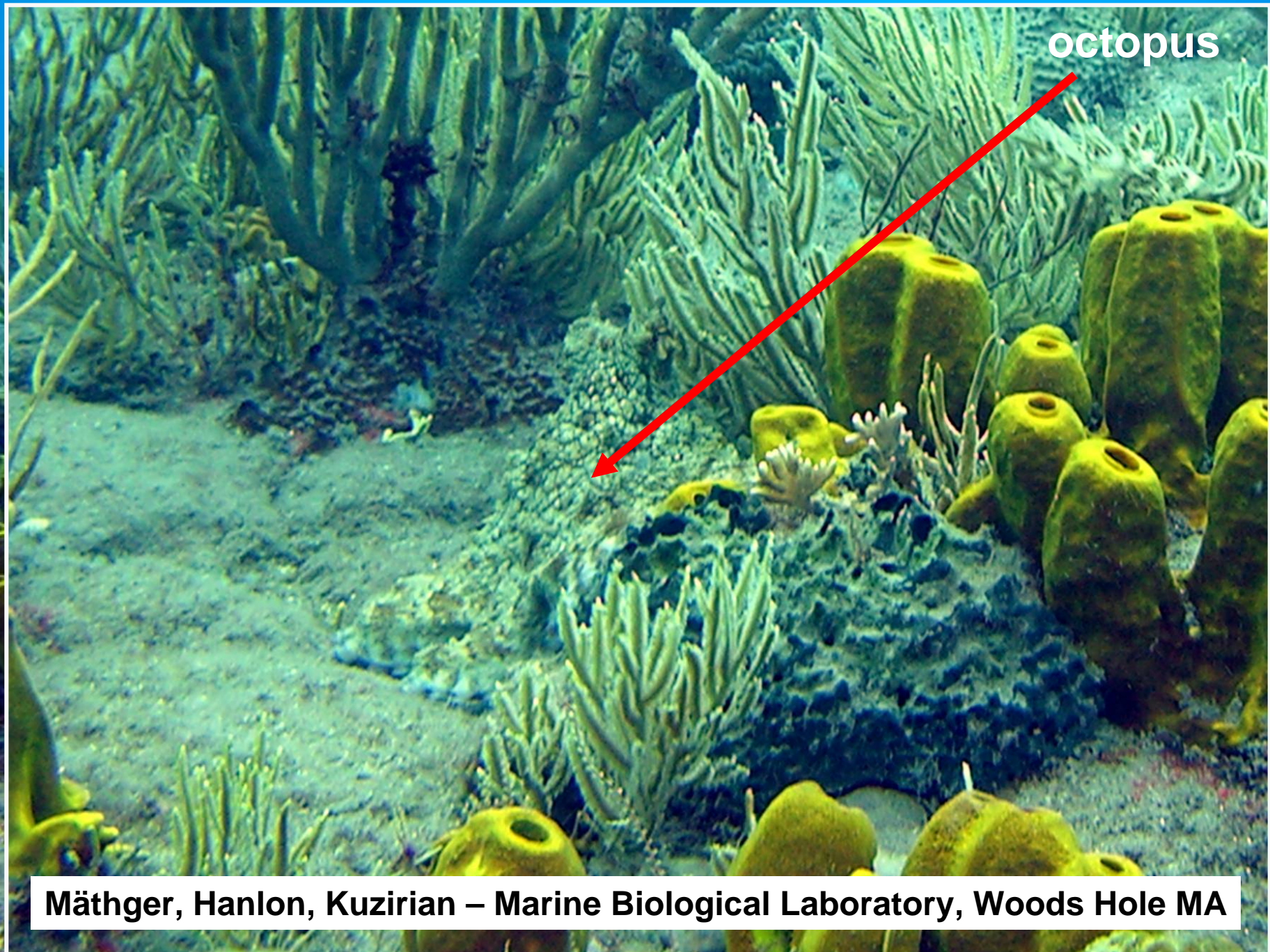
David Beebe



Responsive to
Physiological variables:

- pH
- Salt
- Temperature
- light

- Many stimuli cause deformation.
- Deformation regulates flow.



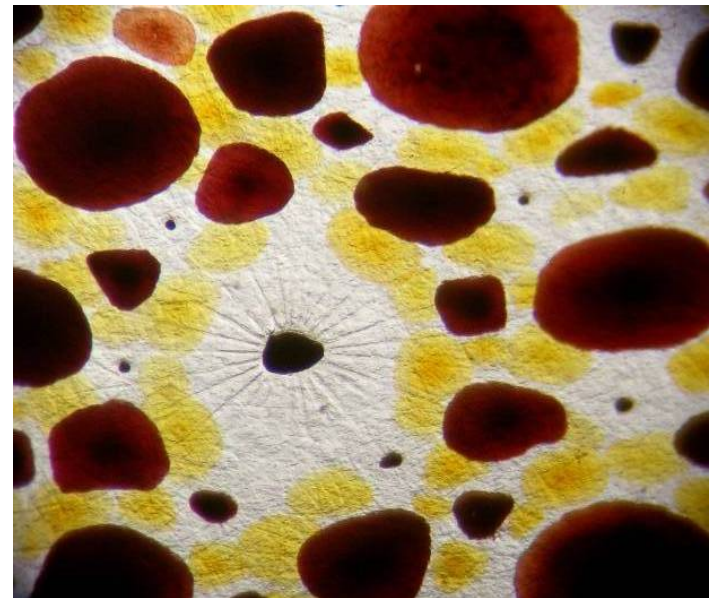
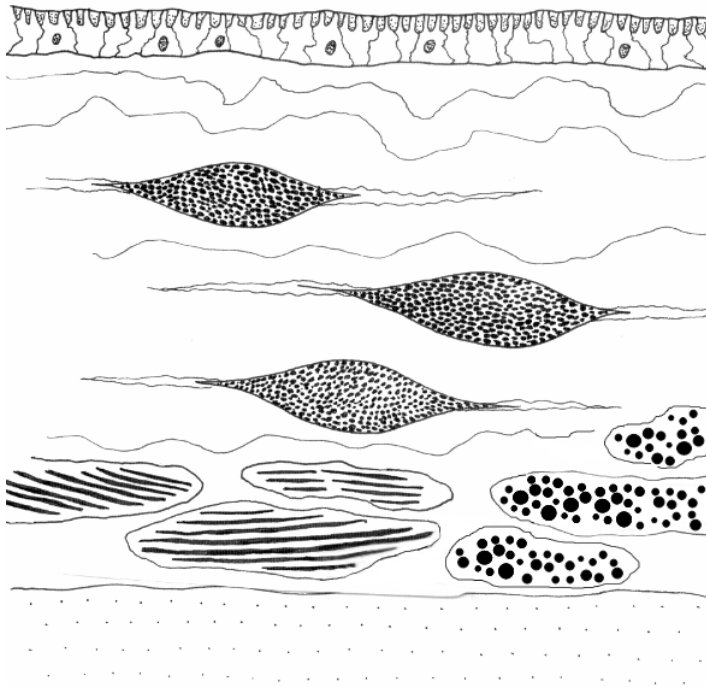
octopus

Mäthger, Hanlon, Kuzirian – Marine Biological Laboratory, Woods Hole MA

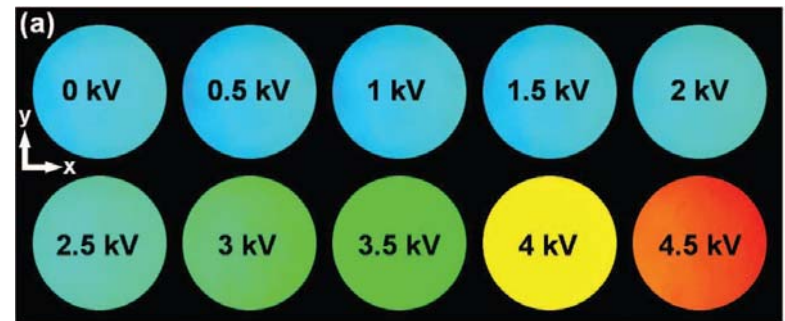
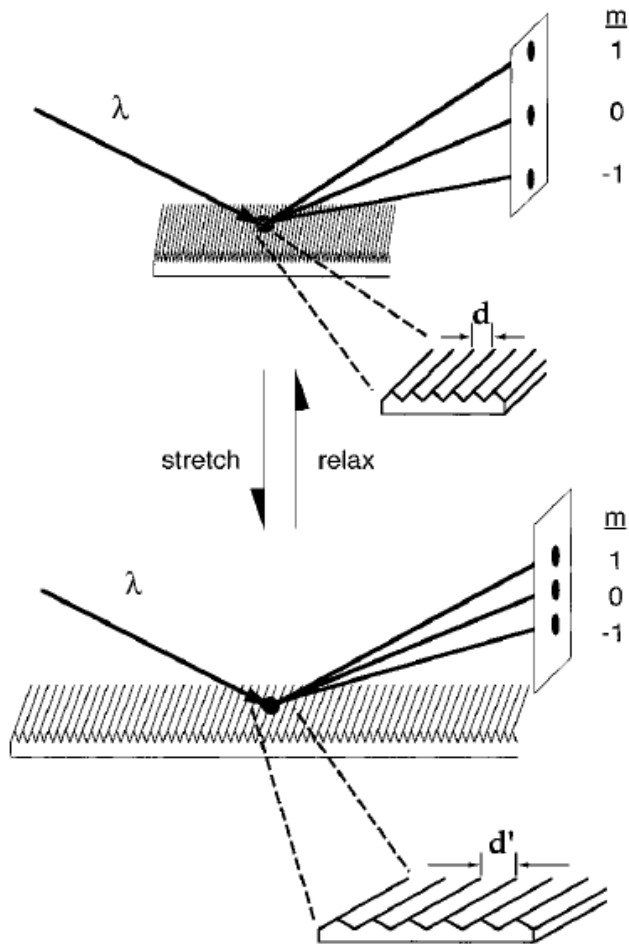
Squid changes color



Expand pigmented sacs by contracting muscles



Adaptive Optics



- Many stimuli cause deformation.
- Deformation affects optics.

Soft Active Materials (SAM)

Soft: large deformation in response to small forces
(rubbers, gels,...)

Active: large deformation in response to diverse stimuli
(electric field, temperature, pH, salt,...)

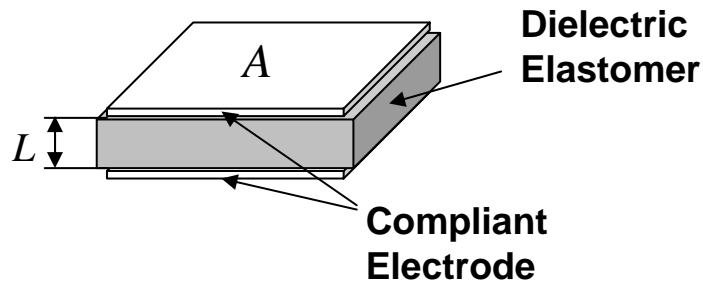
A stimulus causes deformation.

Deformation enables a function.

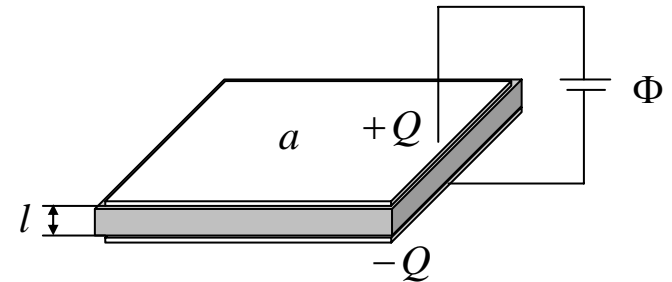


Dielectric elastomer

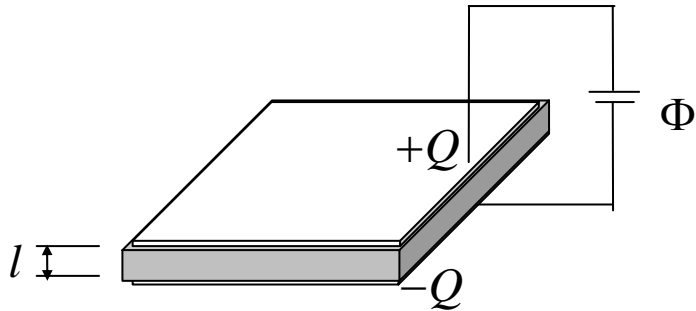
Reference State



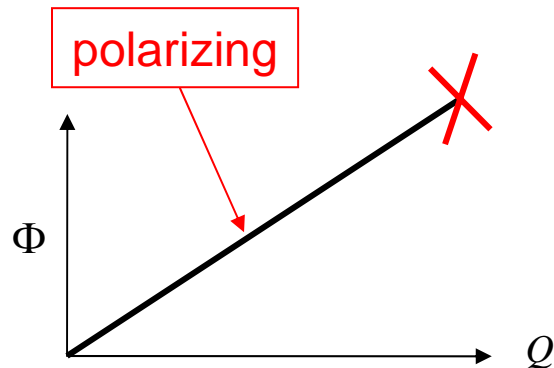
Current State



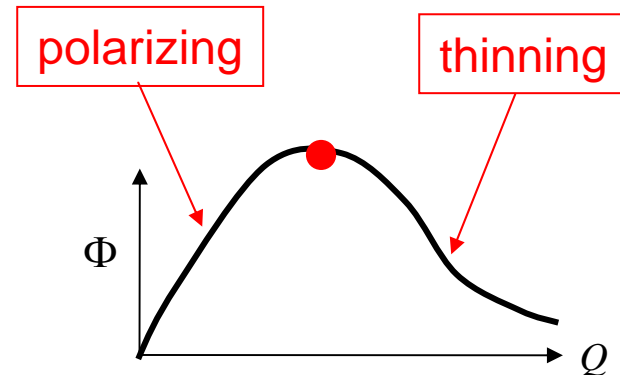
Two modes of failure



Electrical breakdown Hard material



Electromechanical instability Soft material



Stark & Garton, Nature 176, 1225 (1955)

The Essential Dilemma (TED)

- To deform appreciably without electrical breakdown, the elastomer must be soft.
- But a soft elastomer is susceptible to electromechanical instability.

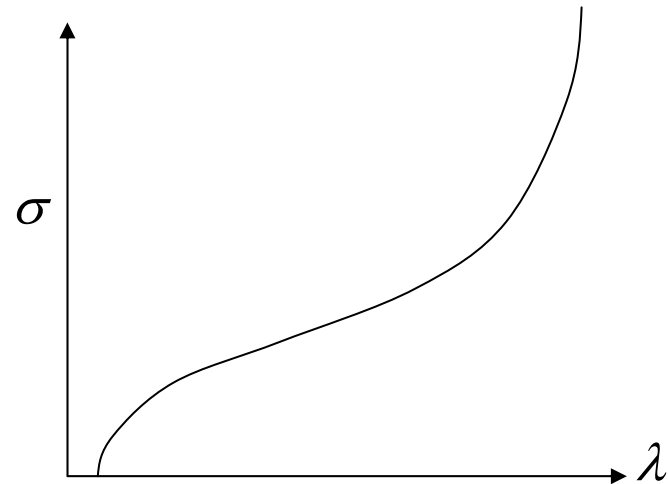
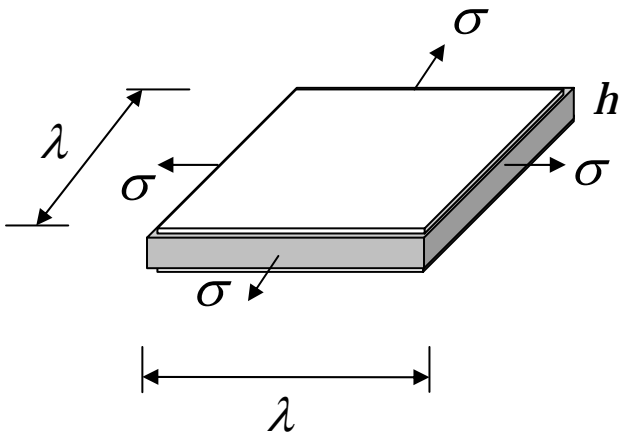
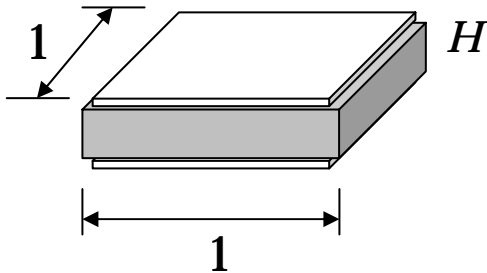
How large can deformation of actuation be?

Experimentally observed large deformation of actuation

- Zhenyi, et al. (1994), ~3%.
- Pelrine, et al. (1998), low modulus, high dielectric strength, ~26%.
- Pelrine, et al. (2000), pre-stress, ~100%.
- Ha, et al. (2006), interpenetrating networks, ~100%.

- How do we understand these experiments?
- What is the theoretical limit?
- How about 1000%?

Mechanics



Equation of state $\sigma = f(\lambda)$

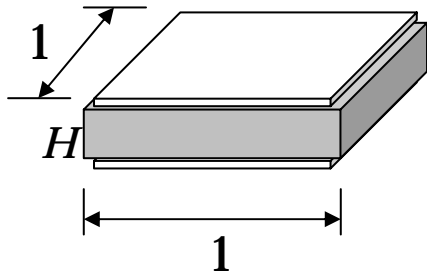
Incompressibility $H = h\lambda^2$

Example:
neo-Hookean model $\sigma = \mu(\lambda^2 - \lambda^{-4})$

Electromechanics

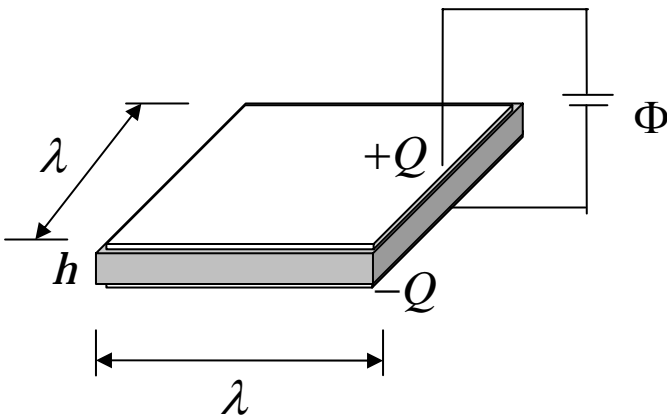
$$H = h\lambda^2$$

$$\sigma = f(\lambda)$$



Maxwell stress $\sigma = \epsilon E^2$

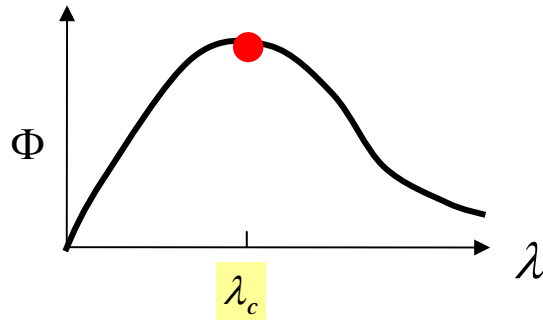
voltage $\Phi = Eh$



Equation of state

$$\Phi = H\lambda^2 \sqrt{\frac{f(\lambda)}{\epsilon}}$$

Electromechanical instability limits deformation of actuation

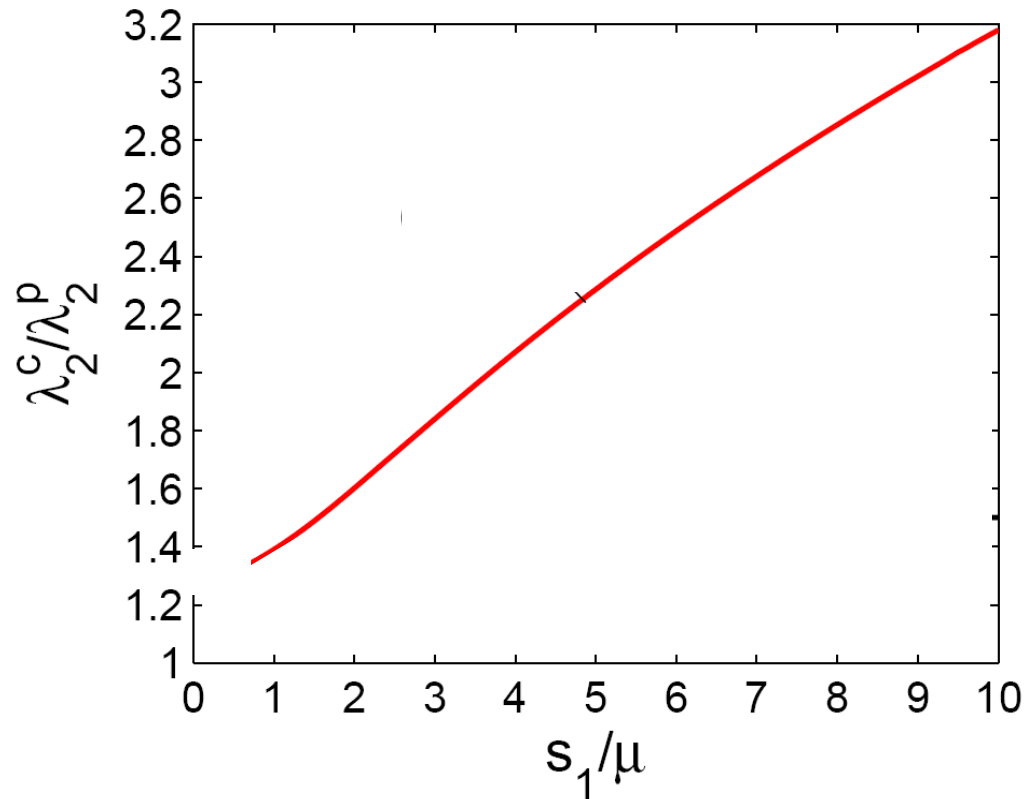
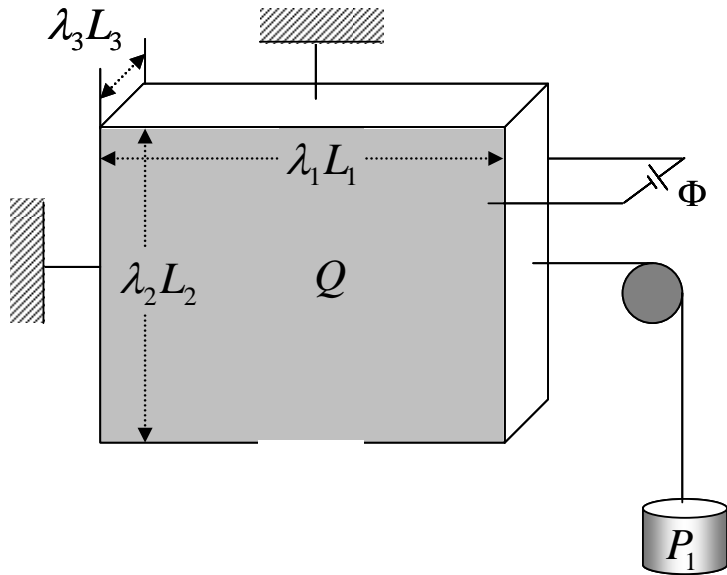


$$\Phi = H \sqrt{\frac{\mu}{\varepsilon}} (\lambda^3 - \lambda^6)^{1/2}$$

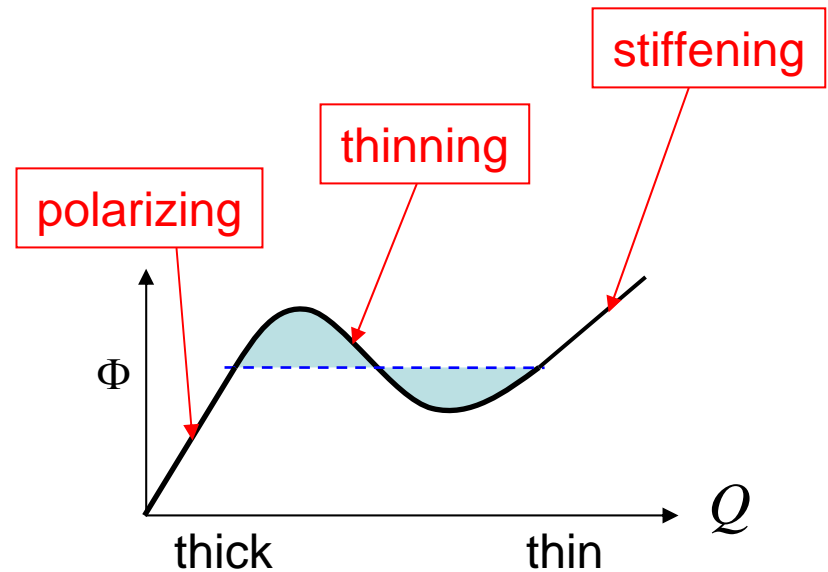
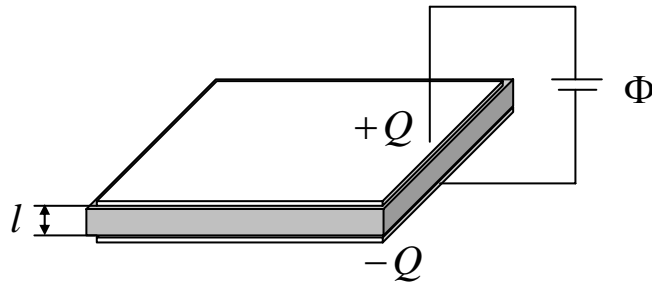
$$\lambda_c = 2^{1/3} \approx 1.26$$

Pre-stretch

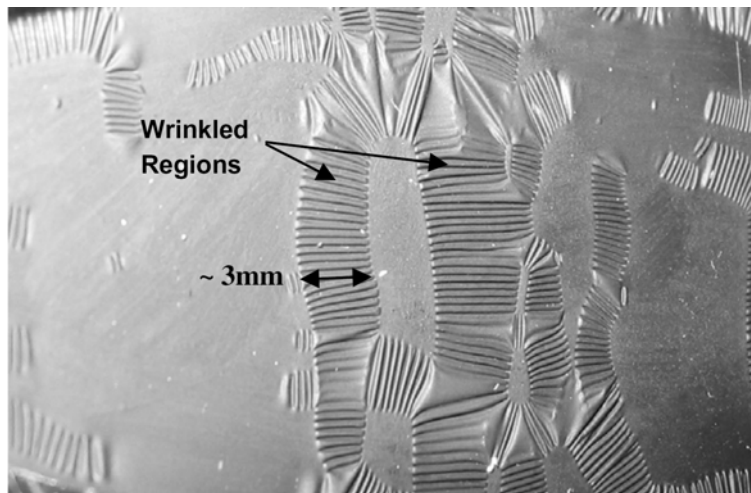
increases deformation of actuation



Coexistent states



Top view



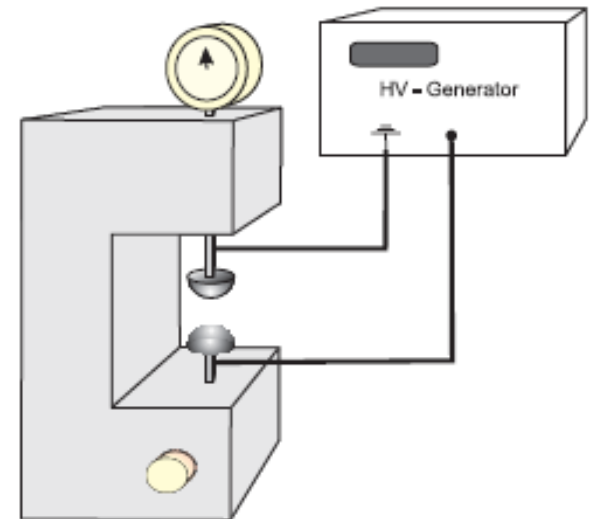
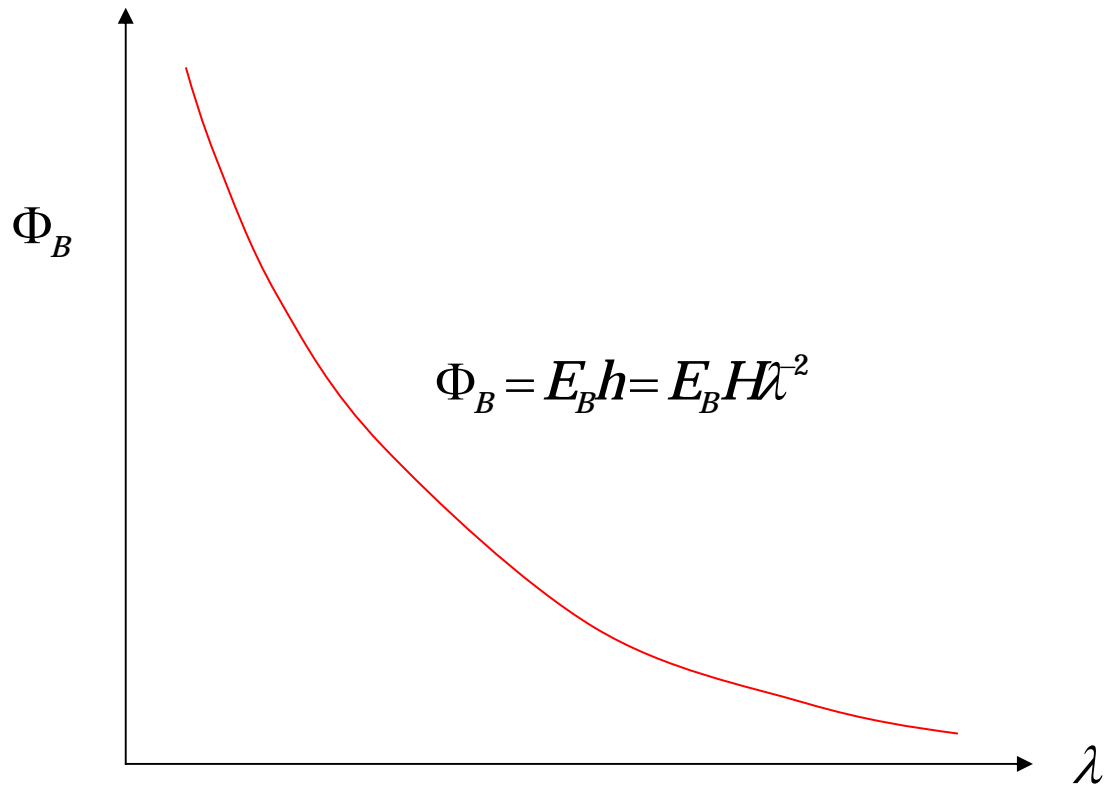
Cross section

Coexistent states: flat and wrinkled

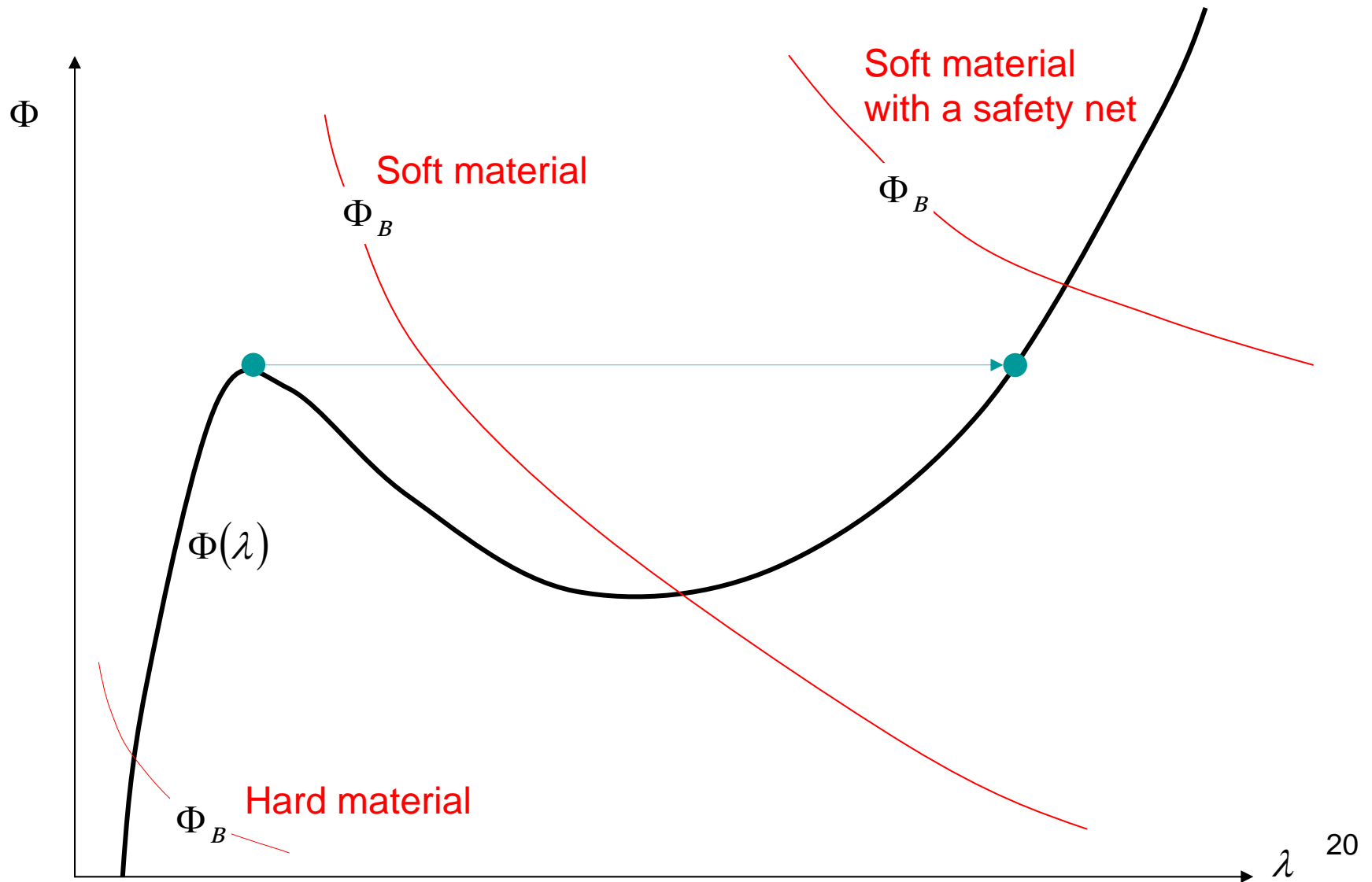
Observation: Plante, Dubowsky,
Int. J. Solids and Structures **43**, 7727 (2006)

Interpretation: Zhao, Hong, Suo
Physical Review B **76**, 134113 (2007)

Electrical breakdown



Snap-through instability may enable an elastomer to achieve giant deformation of actuation



Theoretical limit of deformation of actuation

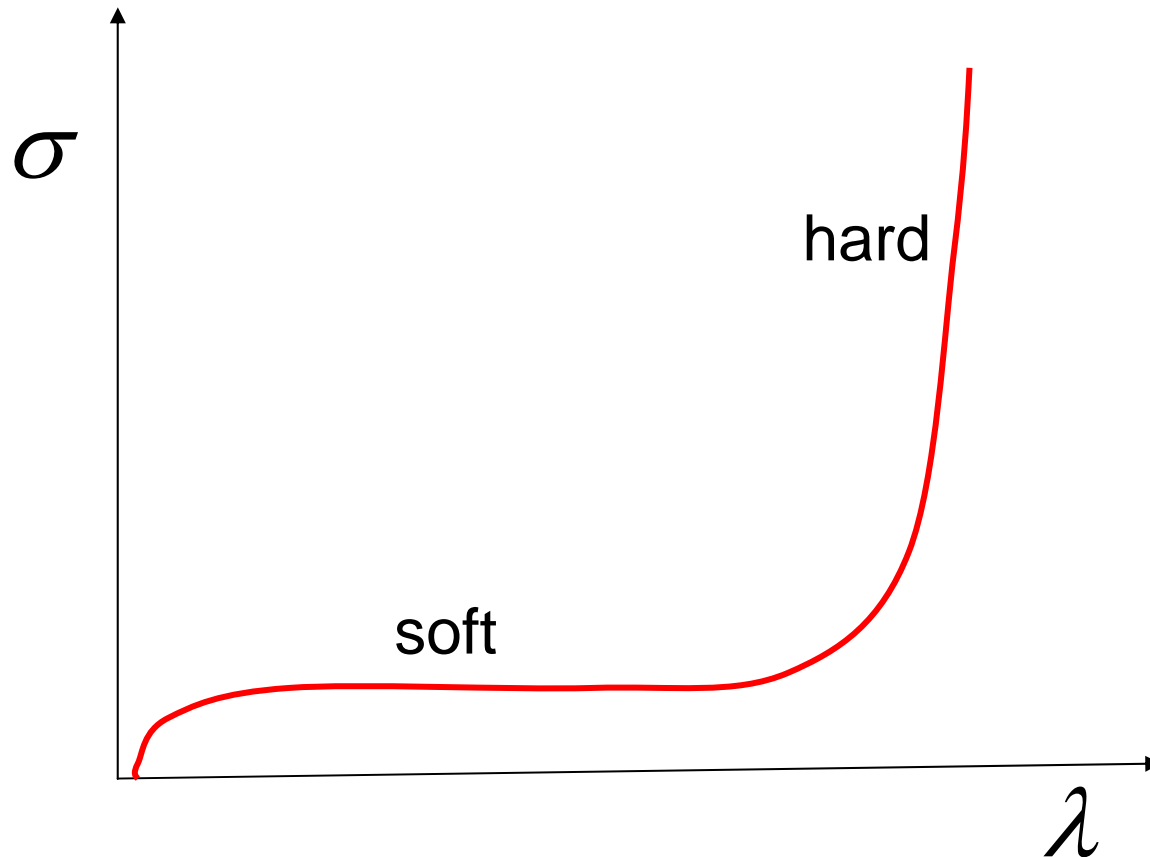
Experimental conditions voltage ramps up;
voltage stays below electrical breakdown, $\Phi_B(\lambda)$

Equations of state
$$\Phi(\lambda) = H\lambda^{-2} \sqrt{\frac{f(\lambda)}{\varepsilon}}$$

Game: Find a material with

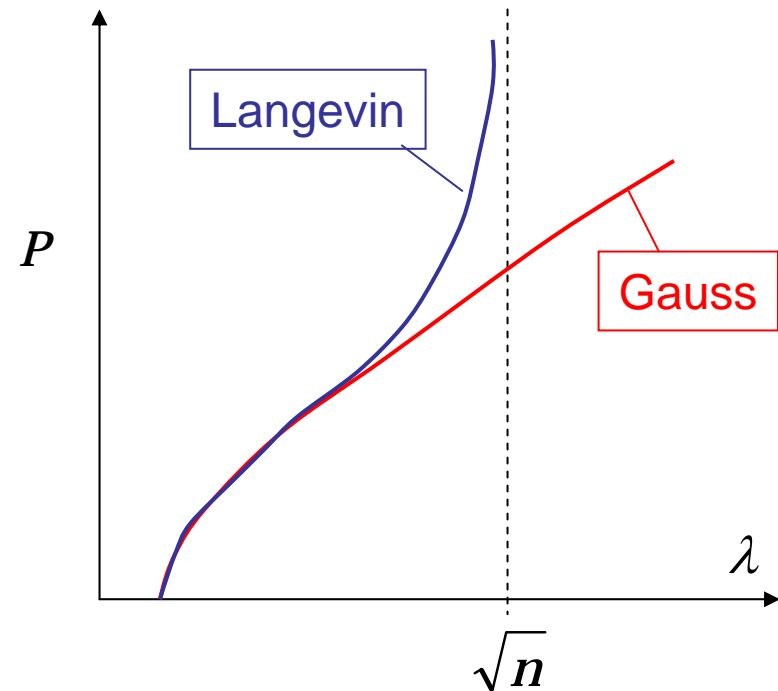
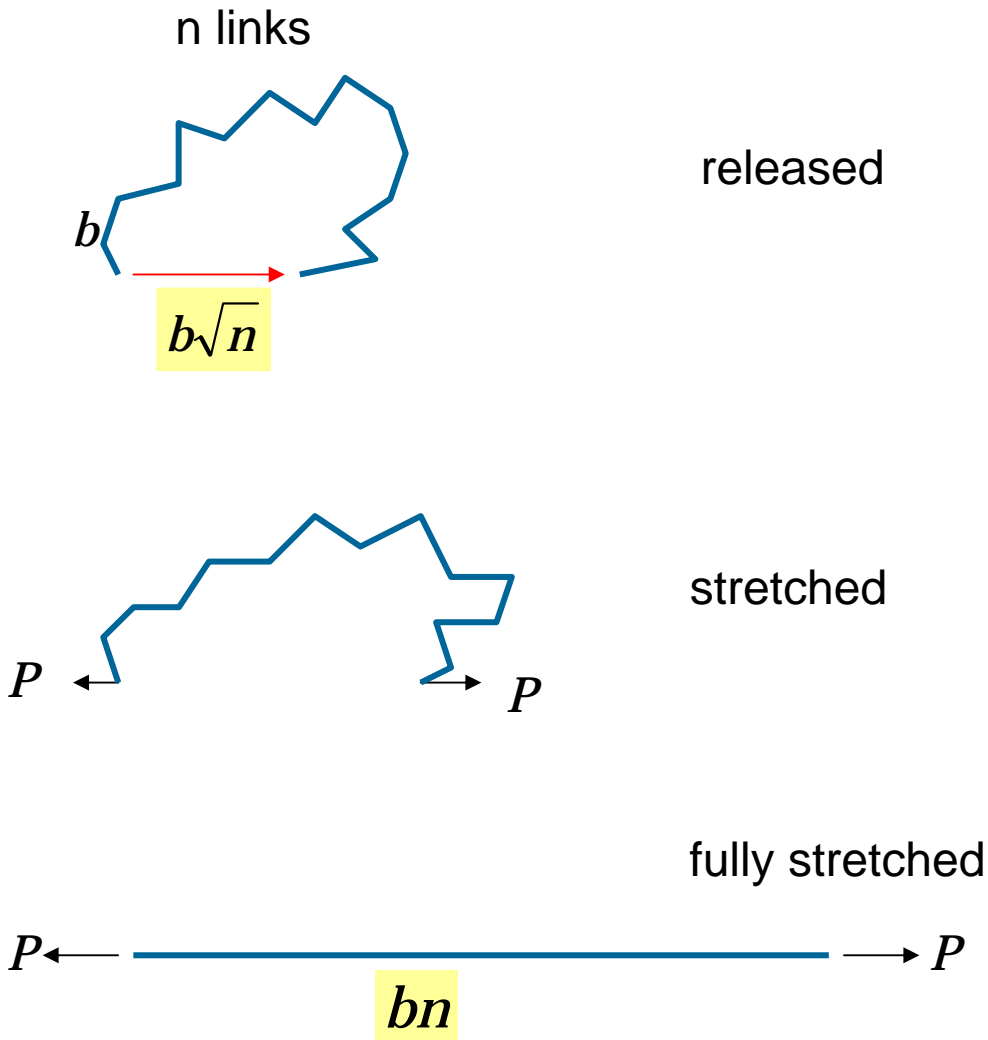
- high dielectric strength,
- suitable stress-strain curve.

Suitable stress-stretch curve

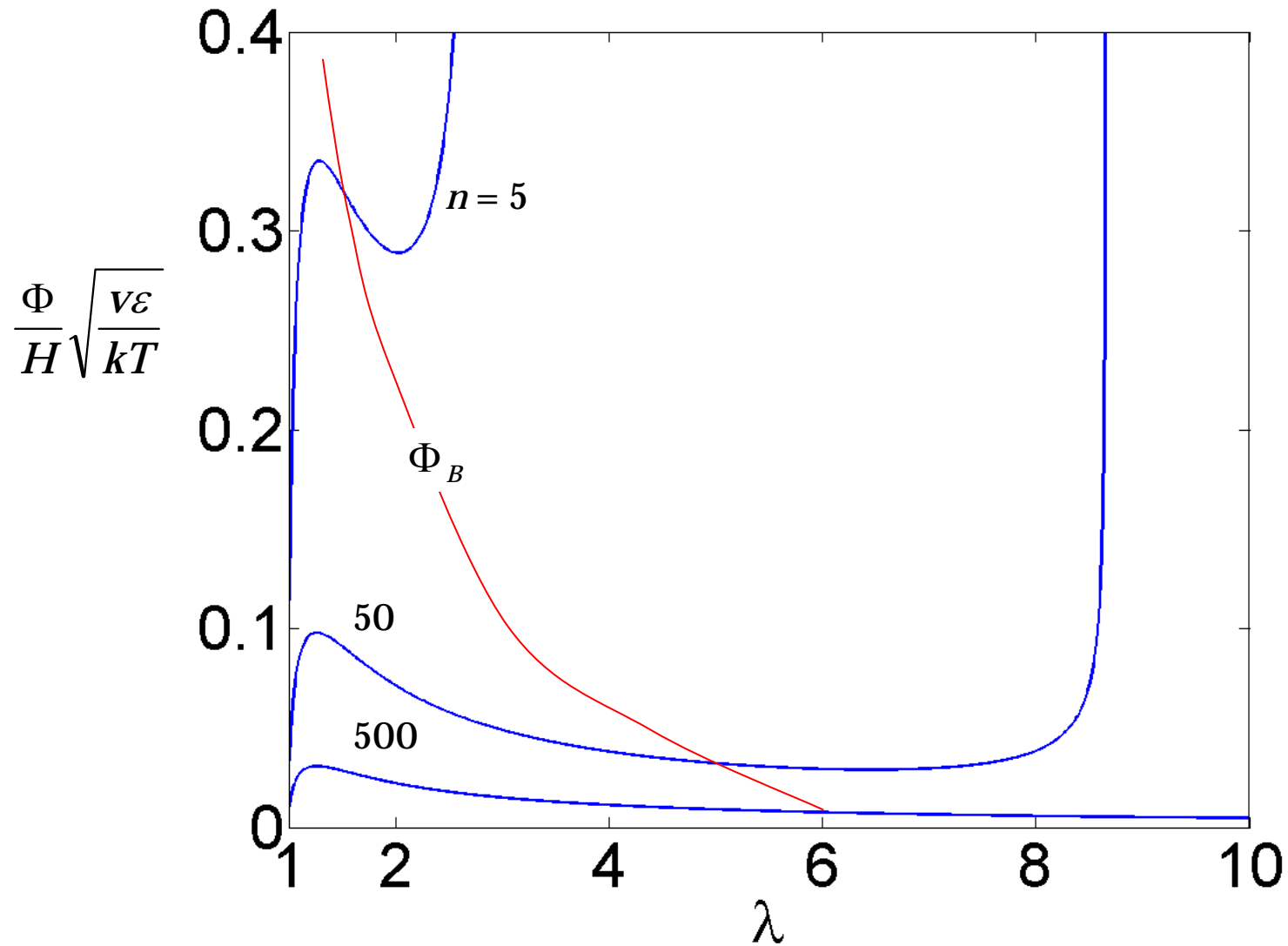


- Soft:** enable large deformation at a voltage below electrical breakdown.
- Hard:** provide a safety net to avert excessive deformation.

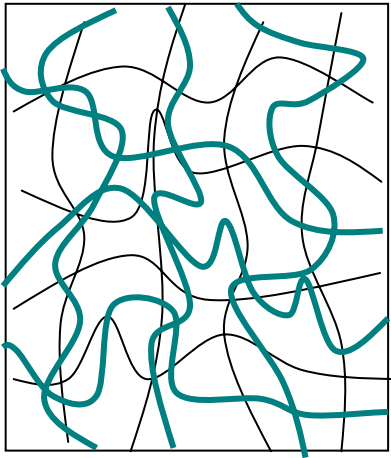
When stretched, a polymer stiffens



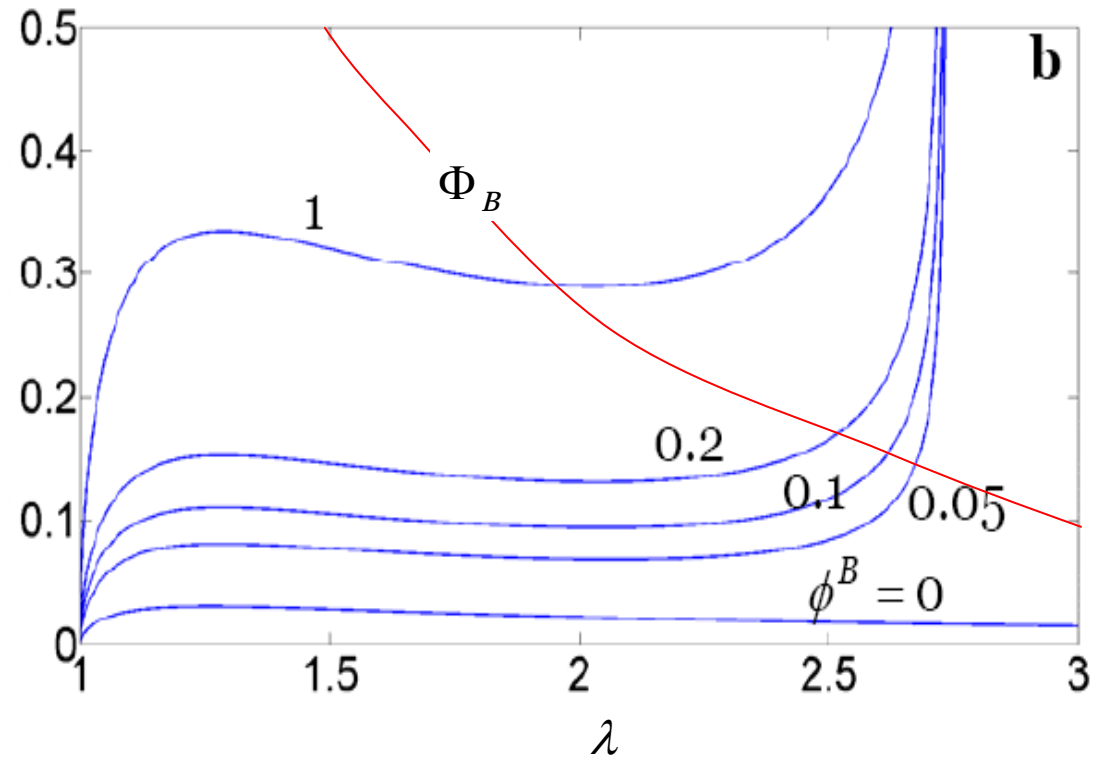
Change chain length



Interpenetrating networks



$$\frac{\Phi}{H} \sqrt{\frac{v\varepsilon}{kT}}$$

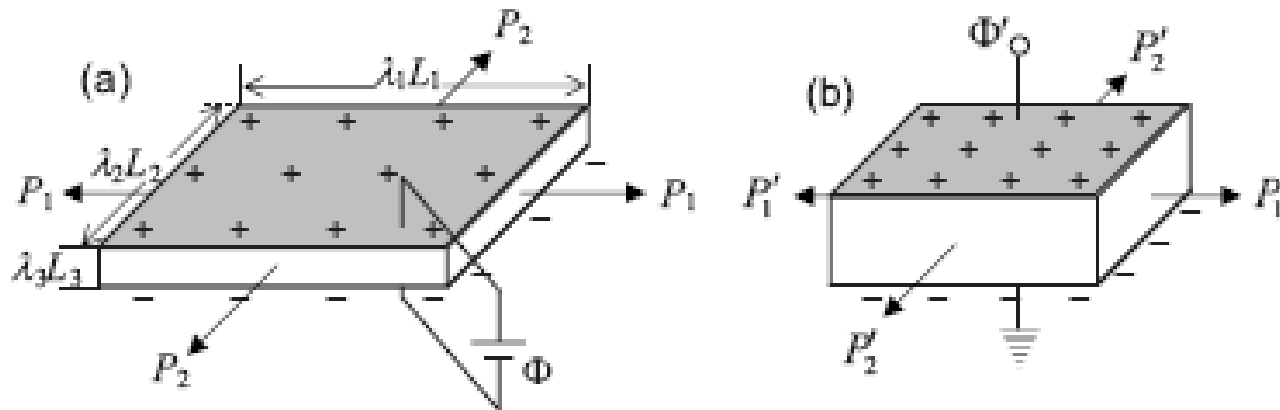


Experiment: Ha, Yuan, Pei, Pelrine
Adv. Mater. 18, 887 (2006).

Theory: Suo, Zhu. APL accepted.

- Short chains provide a safety net.
- Long chains fill the space.

Energy harvesting

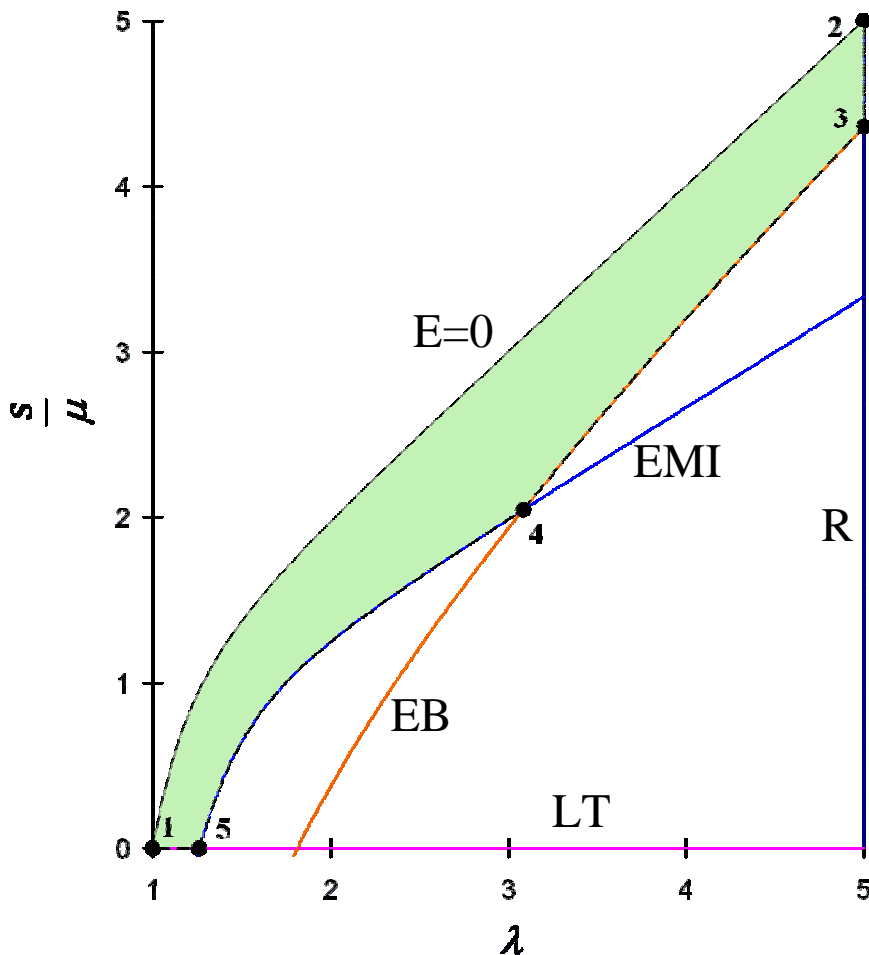


Generate electricity from walking



Generate electricity from ocean waves

Maximal energy that can be converted by a dielectric elastomer



6 J/g, Elastomer (theory)
0.4 J/g, Elastomer (experiment)
0.01 J/g ceramics

Summary: Soft Active Materials

- Many stimuli (E, pH, salt, T...) cause deformation.
- Deformation enables many functions (soft robots, adaptive optics, self-regulating fluidics, programmable haptics, oil recovery, energy harvesting, drug delivery, tissue regeneration, low-cost diagnosis...).
- Snap-through instability may enable an elastomer to achieve giant deformation of actuation.

4 lectures on SAMs: <http://imechanica.org/node/7048>

- Dielectric elastomers
- Neutral gels
- Polyelectrolytes
- pH-sensitive gels